Министерство образования и науки РФ

Федеральное государственное автономное

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«Санкт-Петербургский национальный исследовательский университет

информационных технологий, механики и оптики»

**факультет программной инженерии и компьютерной техники**

**ДОМАШНЯЯ РАБОТА № 6**

по дисциплине

‘Дискретная Математика’

Вариант №12

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Оглавление

[Пункт 1 2](#_Toc93027826)

[Ф1 2](#_Toc93027827)

[Ф2 2](#_Toc93027828)

[Пункт 2 3](#_Toc93027829)

[Ф1 3](#_Toc93027830)

[A > 0, B > 0 3](#_Toc93027831)

[A < 0, B > 0 3](#_Toc93027832)

[A > 0, B < 0 4](#_Toc93027833)

[Ф2 4](#_Toc93027834)

[A > 0, B > 0 5](#_Toc93027835)

[A < 0, B > 0 5](#_Toc93027836)

[A > 0, B < 0 6](#_Toc93027837)

# Пункт 1

A = 0,632

B = 8,287

## Ф1

A = 0,63210 ≈ 0,A1CA16 × 160

ХА = РА + 64 = 6410 = 100 00002

1 округление к ближайшему

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| 0 | 1 | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 1 | 1 | 0 | 0 | 0 | 1 | 1 | 1 | 0 | 1 |
| 0 | 1 |  |  |  |  |  | 7 | 8 |  |  |  |  |  |  |  |  |  |  | 19 |

B = 8,28710 ≈ 8,497816 = 0,8497816 × 161

ХА = РА + 64 = 6510 = 100 00012

1 округление к ближайшему

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| 0 | 1 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 1 | 0 | 0 | 1 |
| 0 | 1 |  |  |  |  |  | 7 | 8 |  |  |  |  |  |  |  |  |  |  | 19 |

## Ф2

A = 0,63210 ≈ 0,1 010 0001 1100 10102 × 2-1

ХА = РА + 128 = 12710 = 0111 11112

1 округление к ближайшему

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| 0 | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 | 0 | 1 | 0 | 0 | 0 | 0 | 1 | 1 | 1 | 0 | 1 |
| 0 |  |  |  |  |  |  |  | 8 | 9 |  |  |  |  |  |  |  |  |  | 19 |

B = 8,28710 ≈ 1000,0100 1001 0111 10002 = 0,1000 0100 1001 0111 10002 × 163

ХА = РА + 128 = 13110 = 1000 00112

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| 0 | 1 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 1 | 0 | 0 | 1 |
| 0 | 1 |  |  |  |  |  |  | 8 | 9 |  |  |  |  |  |  |  |  |  | 19 |

# Пункт 2

## Ф1

|  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- |
| - | XA = | 1 | 0 | 0 | 0 | 0 | 0 | 0 |
| XB = | 1 | 0 | 0 | 0 | 0 | 0 | 1 |
| (XA – XB)доп.= | | 1 | 1 | 1 | 1 | 1 | 1 | 1 |

(XA-XB). = -1

ХС = ХВ = 1.

### A > 0, B > 0

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| 4→ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| MA = | + | . | 0 | 0 | 0 | 0 | 1 | 0 | 1 | 1 | 0 | 0 | 0 | 1 |
| MB = | . | 1 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 1 | 0 | 0 | 1 |
| MC = | 0 | . | 1 | 0 | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 0 | 1 | 0 |

Результат сложения нормализован.

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| С = | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 1 | 1 | 1 | 1 | 1 | 0 | 1 | 0 |
|  | 0 | 1 |  |  |  |  |  | 7 | 8 |  |  |  |  |  |  |  |  |  |  | 19 |

Определим абсолютную и относительную погрешности результата:

С\* = MC \* 16Pc = 0,8FA16 \* 161 = 8,FA16 ≈ 8,97610

∆С = СT – C\* = 8,976 - 8,919 = 0,057

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
| δС = | ∆С | \* 100% = | 0,057 | \* 100% ≈ 0,0006%, |
| СT | 8,919 |

Погрешность полученного результата объясняется неточным представлением операндов.

### A < 0, B > 0

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| MB = | - | . | 1 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 1 | 0 | 0 | 1 |
| 4→ |  |  |  |  |  |  |  |  |  |  |  |  |  |
| MA = | . | 0 | 0 | 0 | 0 | 1 | 0 | 1 | 1 | 0 | 0 | 0 | 1 |
| MC = | 0 | . | 0 | 1 | 1 | 1 | 1 | 0 | 0 | 1 | 1 | 0 | 0 | 0 |

Результат вычитания нормализован.

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| С = | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 1 | 1 | 1 | 1 | 0 | 0 | 1 | 1 | 0 | 0 | 0 |
|  | 0 | 1 |  |  |  |  |  | 7 | 8 |  |  |  |  |  |  |  |  |  |  | 19 |

Определим абсолютную и относительную погрешности результата:

С\* = MC \* 16Pc = 0,79816 \* 161 = 7,9816 = 7,5937510

∆С = СT – C\* = 7,655 – 7,59375 = 0,06125

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
| δС = | ∆С | \* 100% = | 0.06125 | \* 100% ≈ 0,8%, |
| СT | 7,655 |

Погрешность полученного результата объясняется неточным представлением операндов.

### A > 0, B < 0

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| 4→ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| MA = | - | . | 0 | 0 | 0 | 0 | 1 | 0 | 1 | 1 | 0 | 0 | 0 | 1 |
| MB = | . | 1 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 1 | 0 | 0 | 1 |
| MC = | 1 | . | 1 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 1 | 0 | 0 | 0 |

Результат сложения нормализован и представлен в дополнительном коде.

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| С = | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 1 | 1 | 1 | 1 | 0 | 0 | 1 | 1 | 0 | 0 | 0 |
|  | 0 | 1 |  |  |  |  |  | 7 | 8 |  |  |  |  |  |  |  |  |  |  | 19 |

Определим абсолютную и относительную погрешности результата:

С\* = MC \* 16Pc = -0,79816 \* 161 = -7,9816 = -7,5937510

∆С = СT – C\* = 7,655 – 7,59375 = 0,06125

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
| δС = | ∆С | \* 100% = | 0.06125 | \* 100% ≈ 0,8%, |
| СT | 7,655 |

Погрешность полученного результата объясняется неточным представлением операндов.

## Ф2

|  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| - | XA = | 0 | 1 | 1 | 1 | 1 | 1 | 1 | 1 |
| XB = | 1 | 0 | 0 | 0 | 0 | 0 | 1 | 1 |
| (XA – XB)доп.= | | 0 | 0 | 0 | 0 | 0 | 0 | 1 | 0 |

(XA-XB). = 2

ХС = ХВ = 3

### A > 0, B > 0

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| 2→ |  |  |  |  |  |  |  |  |  |  |  |  |  |
| MA = | + | . | 0 | 0 | 0 | 1 | 0 | 0 | 0 | 0 | 1 | 1 | 1 |
| MB = | . | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 1 | 0 | 0 | 1 |
| MC = | 0 | . | 0 | 0 | 0 | 1 | 1 | 0 | 1 | 0 | 0 | 0 | 0 |

Результат сложения нормализован.

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| С = | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 0 | 0 | 1 | 1 | 0 | 1 | 0 | 0 | 0 | 0 |
|  | 0 | 1 |  |  |  |  |  |  | 8 | 9 |  |  |  |  |  |  |  |  |  | 19 |

Определим абсолютную и относительную погрешности результата:

С\* = MC \* 2Pc = 0,1000 11012 \* 24 = 1000,11012 ≈ 8,97610

∆С = СT – C\* = 8,976 - 8,919 = 0,057

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
| δС = | ∆С | \* 100% = | 0,057 | \* 100% ≈ 0,0006%, |
| СT | 8,919 |

Погрешность полученного результата объясняется неточным представлением операндов.

### A < 0, B > 0

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| MB = | - | . | 1 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 1 | 0 | 0 | 1 |
| 4→ |  |  |  |  |  |  |  |  |  |  |  |  |  |
| MA = | . | 0 | 0 | 0 | 0 | 1 | 0 | 1 | 1 | 0 | 0 | 0 | 1 |
| MC = | 0 | . | 0 | 1 | 1 | 1 | 1 | 0 | 0 | 1 | 1 | 0 | 0 | 0 |

Результат вычитания нормализован.

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| С = | 0 | 1 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 1 | 1 | 1 | 1 | 0 | 0 | 1 | 1 | 0 | 0 | 0 |
|  | 0 | 1 |  |  |  |  |  | 7 | 8 |  |  |  |  |  |  |  |  |  |  | 19 |

Определим абсолютную и относительную погрешности результата:

С\* = MC \* 16Pc = 0,79816 \* 161 = 7,9816 = 7,5937510

∆С = СT – C\* = 7,655 – 7,59375 = 0,06125

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
| δС = | ∆С | \* 100% = | 0.06125 | \* 100% ≈ 0,8%, |
| СT | 7,655 |

Погрешность полученного результата объясняется неточным представлением операндов.

### A > 0, B < 0

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| 4→ |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| MA = | - | . | 0 | 0 | 0 | 0 | 1 | 0 | 1 | 1 | 0 | 0 | 0 | 1 |
| MB = | . | 1 | 0 | 0 | 0 | 0 | 1 | 0 | 0 | 1 | 0 | 0 | 1 |
| MC = | 1 | . | 1 | 0 | 0 | 0 | 0 | 1 | 1 | 0 | 1 | 0 | 0 | 0 |

Результат сложения нормализован и представлен в дополнительном коде.

|  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |  |
| --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- | --- |
| С = | 1 | 1 | 0 | 0 | 0 | 0 | 0 | 1 | 0 | 1 | 1 | 1 | 1 | 0 | 0 | 1 | 1 | 0 | 0 | 0 |
|  | 0 | 1 |  |  |  |  |  | 7 | 8 |  |  |  |  |  |  |  |  |  |  | 19 |

Определим абсолютную и относительную погрешности результата:

С\* = MC \* 16Pc = -0,79816 \* 161 = -7,9816 = -7,5937510

∆С = СT – C\* = 7,655 – 7,59375 = 0,06125

|  |  |  |  |  |
| --- | --- | --- | --- | --- |
| δС = | ∆С | \* 100% = | 0.06125 | \* 100% ≈ 0,8%, |
| СT | 7,655 |

Погрешность полученного результата объясняется неточным представлением операндов.